



## Predicting methane emissions of lactating Danish Holstein cows using Fourier transform mid-infrared spectroscopy of milk

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### ABSTRACT

Enteric methane (CH<sub>4</sub>), a potent greenhouse gas, is among the main targets of mitigation practices for the dairy industry. A measurement technique that is rapid, inexpensive, easy to use, and applicable at the population level is desired to estimate CH<sub>4</sub> emission from dairy cows. In the present study, feasibility of milk Fourier transform mid-infrared (FT-IR) spectral profiles as a predictor for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production (L/d) is explained. The partial least squares regression method was used to develop the prediction models. The models were validated using different random test sets, which are independent from the training set by leaving out records of 20% cows for validation and keeping records of 80% of cows for training the model. The data set consisted of 3,623 records from 500 Danish Holstein cows from both experimental and commercial farms. For both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production, low prediction accuracies were found when models were obtained using FT-IR spectra. Validated coefficient of determination ( $R^2_{\text{Val}}$ ) = 0.21 with validated model error root mean squared error of prediction (RMSEP) = 0.0114 L/d for CH<sub>4</sub>:CO<sub>2</sub> ratio, and  $R^2_{\text{Val}}$  = 0.13 with RMSEP = 111 L/d for CH<sub>4</sub> production. The important spectral wavenumbers selected using the recursive partial least squares method represented major milk components fat, protein, and lactose regions of the spectra. When fat and protein predicted by FT-IR were used instead of full spectra, a low  $R^2_{\text{Val}}$  of 0.07 was obtained for both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production prediction. Other spectral wavenumbers related to lactose (carbohydrate) or additional wavenumbers related to fat or protein (amide II) are providing additional variation when using the full spectral profile. For CH<sub>4</sub>:CO<sub>2</sub> ratio prediction, integration of FT-IR with other factors such as milk yield, herd, and lactation stage showed improvement in the prediction accuracy. However, overall

prediction accuracy remained modest;  $R^2_{\text{Val}}$  increased to 0.31 with RMSEP = 0.0105. For prediction of CH<sub>4</sub> production, the added value of FT-IR along with the aforementioned traits was marginal. These results indicated that for CH<sub>4</sub> production prediction, FT-IR profiles reflect primarily information related to milk yield, herd, and lactation stage rather than individual milk fatty acids related to CH<sub>4</sub> emission. Thus, it is not feasible to predict CH<sub>4</sub> emission based on FT-IR spectra alone.

**Key words:** CH<sub>4</sub> production, CH<sub>4</sub>:CO<sub>2</sub> ratio, infrared spectroscopy, prediction, validation

### INTRODUCTION

Methane (CH<sub>4</sub>) emissions are of concern because of the observed climate change effects. Methane, a potent greenhouse gas that contributes substantially to global warming, accounts for approximately 52% of the greenhouse gas emissions in both developing and developed countries (FAO, 2010). Enteric CH<sub>4</sub> composes 17% of global methane and is therefore the single largest source of anthropogenic CH<sub>4</sub> (Knapp et al., 2014). Agriculture is considered to be the major producer of anthropogenic CH<sub>4</sub>, and most CH<sub>4</sub> is naturally emitted by dairy cows during the microbial fermentation of feed components (Gerber et al., 2013). In addition to its relevance on climate impact, the eructed CH<sub>4</sub> induces a significant loss of gross energy intake as CH<sub>4</sub> reduces the availability of consumed energy for the cow (Johnson and Johnson, 1995).

Thus, mitigating CH<sub>4</sub> emissions seems to be an obvious approach to improving sustainability and profitability of dairy production. Measurement techniques applicable on a large scale to estimate specific amounts of CH<sub>4</sub> emitted by a cow would therefore be valuable. Several techniques have been developed to measure enteric CH<sub>4</sub> emissions (Patra, 2016). However, in practice, recording CH<sub>4</sub> emission is expensive and difficult for a large population. Milk Fourier transform mid-infrared (FT-IR) profile may be useful as an indicator trait for CH<sub>4</sub> emission. Milk FT-IR spectral data are rou-

Received April 12, 2017.

Accepted July 26, 2017.

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tinely generated for all individual milk samples; if it is feasible to predict CH<sub>4</sub> emission using FT-IR, the prediction can be obtained at the population level at no additional cost. Globally, FT-IR spectroscopy has been used for decades at commercial milk recording agencies and dairies for routine quantification of the major milk components fat, protein, and lactose content. Several studies have investigated the potential use of milk FT-IR spectroscopy to predict detailed milk quality traits such as individual milk fatty acids (FA) and proteins (De Marchi et al., 2014). Recently, numerous studies have also focused on the use of FT-IR spectroscopy to predict animal-related characteristics such as energy status (intake and balance), residual feed intake (McParland et al., 2011, 2012, 2014), and CH<sub>4</sub> emission (Dehareng et al., 2012; Vanlierde et al., 2015, 2016).

The objective of the present study was to evaluate the feasibility of FT-IR spectroscopy of milk to predict CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production in lactating Danish Holstein cows. We investigated the added value of milk FT-IR spectroscopy in the prediction of CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production. The present study used a considerably larger data set to develop the prediction models compared with preceding studies (Dehareng et al., 2012; Vanlierde et al., 2015, 2016). Moreover, the robustness of generated prediction models was validated using different random test sets that are independent from the training set.

## MATERIALS AND METHODS

### Data Collection

Data were collected from the Danish Cattle Research Centre (DCRC; Foulum, Denmark) and 2 Danish commercial farms (referred to as A and B). In total, 215 Danish Holstein cows from DCRC and 285 Danish Holstein cows from commercial farms had CH<sub>4</sub> measurements and corresponding FT-IR spectral profile. Milk samples were collected at DCRC and commercial herds and sent to the Eurofins-Steins laboratory (Vejen, Denmark) for FT-IR spectral analyses using a MilkoScan FT+ (Foss, Hillerød, Denmark). For DCRC, CH<sub>4</sub> measurements were taken April 2015 to September 2016. For commercial farms, herd A consisted of 158 cows, and CH<sub>4</sub> measurements were performed October 2015 to January 2016; herd B consisted of 127 cows, and CH<sub>4</sub> measurements were taken during February and March 2016.

Total data analyzed included 3,623 CH<sub>4</sub>:CO<sub>2</sub> ratio records from 500 cows and 2,202 CH<sub>4</sub> production (L/d) records from 490 cows. Some values for CH<sub>4</sub> production were missing due to the missing insemination date information, which was used in the calculation of predicted

CO<sub>2</sub> (Madsen et al., 2010) and then used to calculate CH<sub>4</sub> production. For DCRC data the FT-IR spectral data records representing 2 to 6 milk samples per week per cow were averaged on a weekly basis corresponding to the weekly available CH<sub>4</sub> records. At commercial farms approximately 1 spectrum per month per cow (standard milk control sample) was available; therefore, the raw spectra corresponding to the week of CH<sub>4</sub> measurement were considered for the analysis. Effects of using weekly averaged FT-IR spectra versus raw spectral data were evaluated by building prediction models for fat and protein. Prediction results did not differ when using weekly averaged versus raw spectral profile for both fat and protein contents. However, this could be different for CH<sub>4</sub> production if CH<sub>4</sub> is more variable with day-to-day changes. Additional traits such as weekly averages for daily milk yield (MY; kg/d), herd, parity, lactation stage, season, weekly averaged fat, and protein content were used as predictor traits for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production.

Lactation stage included 1 to 44 wk and is described using a Wilmlink exponential function (Wilmlink, 1987). Seasonal variation is described using a Fourier series approach with sine and cosine functions of day of the year (previously used by Løvendahl and Bjerring, 2006).

### Reference Data

At DCRC, CH<sub>4</sub> and CO<sub>2</sub> gas concentrations (in ppm) from breath samples were analyzed using the noninvasive “sniffer” method. At DCRC nondispersive infrared (NDIR) gas analyzers were installed within each automated milking station (AMS; Guardian NG/Gascard, Edinburgh Instruments Ltd., Livingston, UK) and at commercial farms using both NDIR and the portable Fourier transform infrared analyzer (Gasmeter DX 4000, Gasmeter Technologies Oy, Helsinki, Finland. Difford et al. (2016) demonstrated how measurements of CH<sub>4</sub> and CO<sub>2</sub> from both instruments can be used interchangeably. Thus, it was possible to combine the data from DCRC and commercial farms.

The CH<sub>4</sub> and CO<sub>2</sub> gas concentrations for each cow milking in the AMS were corrected for ambient barn concentrations and diurnal variation and averaged over a full week of lactation to calculate the CH<sub>4</sub>:CO<sub>2</sub> ratio (Lassen et al., 2012). The barn concentrations were estimated from the ambient concentrations within the AMS during the morning cleaning cycle when no cows were present. The ECM, BW, and gestation length of each cow were used to estimate heat production (CIGR, 2002), which was converted to CO<sub>2</sub> production (Pedersen et al., 2008) and multiplied by CH<sub>4</sub>:CO<sub>2</sub> as recommended by Madsen et al. (2010) to generate CH<sub>4</sub> production (L/d). The BW was calculated as the aver-

age BW from all milkings in the AMS over the week of measurement. The ECM was calculated as the average MY during the week of measurement corrected for fat, protein, and lactose content, which were estimated from the FT-IR spectra during the week of measurement (Sjaunja et al., 1990).

### Prediction Model Development

Data were analyzed using MATLAB (version R2015a; The MathWorks, Natick, MA) along with PLS toolbox (Eigenvector Research Inc., Manson, WA). The FT-IR spectral data represented infrared light transmittance through the milk sample at wavenumber regions (frequencies) ranging from 925 to 5,008  $\text{cm}^{-1}$ , which comprises 1,060 wavenumbers. The spectra were transformed from transmittance to absorbance to obey Beer's law (Swinehart, 1962). To improve the repeatability of the measurement, 241 spectral data points from 3 spectral regions (1,000–1,550  $\text{cm}^{-1}$ , 1,705–1,820  $\text{cm}^{-1}$ , and 2,700–2,955  $\text{cm}^{-1}$ ) were retained for the analyses, and remaining uninformative spectral regions together with high water absorption, O–H stretching (between  $\sim 1,600$  and  $1,700 \text{ cm}^{-1}$ ), and O–H bending ( $>3,005 \text{ cm}^{-1}$ ) regions were omitted (Eskildsen et al., 2014).

The partial least squares regression (PLSR) method (Wold et al., 1983; Martens and Naes, 1989) was used to develop the prediction models. The method has been widely used in quantitative spectroscopy to determine a relationship between spectral profile (i.e., predictors), which is collinear in nature, and related chemical or physical data (i.e., predictants). Models were developed with and without preprocessing the spectral data. The literature showed quite similar results when different preprocessing is applied to milk FT-IR spectra. One study showed better accuracies using the Savitzky–Golay derivative (Savitzky and Golay, 1964) compared with untreated spectral data, and in another study better accuracies were found using untreated data (De Marchi et al., 2014). Therefore, in the present study models were tested using both untreated data and Savitzky–Golay first derivatives with filter width 7 and polynomial order 2. Prediction models were developed using different combinations of predictor variables, namely FT-IR spectra, MY, parity, herd, lactation stage, and season. Variables with different units were equally scaled using the autoscaling method.

Optimal PLSR components were chosen based on the lowest root mean squared error of cross-validation value using 10 random iterations; this was to avoid over- or underfitting in the final PLSR model. Partial least squares regression Hotelling  $T^2$  versus Q-residual

plots were used for outlier analysis. Coefficients of determination for validation ( $R^2_{\text{val}}$ ) and coefficients of determination for calibration along with model error root mean squared error of calibration and prediction (RMSEP; Esbensen, 2000) were used to evaluate the predictive ability of the obtained calibration models.

Both experimental (i.e., DCRC) and commercial farm data were combined to increase variation in data. The robustness of the obtained prediction model was evaluated using different test sets that are independent from the training set (external test sets). For  $\text{CH}_4:\text{CO}_2$  ratio, out of the 500 cows, 20% ( $n = 100$  cows) were randomly left out for validation and the remaining 80% ( $n = 400$  cows) were used to train the model. For  $\text{CH}_4$  production, out of the 490 cows, 20% ( $n = 98$  cows) were randomly left out for validation and the remaining 80% ( $n = 392$  cows) were used to train the model. In total, 50 random iterations were performed to compare the models for robustness.

### Variable Selection

Important spectral variables were identified using the variable importance for projection (VIP) method and the recursive weighted partial least squares (rPLS) variable selection method (Rinnan et al., 2014). Variable importance for projection is a measure of how well a variable contributes to describing both predictors and response variables. A variable with a VIP score  $>1$  indicates importance for the developed PLSR model (Andersen and Bro, 2010). In rPLS, the regression coefficients are used as weights on the original data matrix. The procedure is based on repeated PLS models, and the rPLS method iteratively uses the regression coefficients to boost important variables and thus relatively downweight less important ones. Therefore, the rPLS model helps identify most specific wavenumbers of important FT-IR regions. Large absolute weights indicate important variables, and weights close to zero indicate less important variables (Rinnan et al., 2014).

## RESULTS

### Data Description

Descriptive statistics of the  $\text{CH}_4:\text{CO}_2$  ratio and  $\text{CH}_4$  production (L/d) are shown in Table 1. Average  $\text{CH}_4:\text{CO}_2$  ratio was 0.069 (SD = 0.013), and average  $\text{CH}_4$  production was 437 L/d (SD = 119 L/d). Table 2 gives the Pearson correlations between different predictor traits and  $\text{CH}_4$  measurements. Milk yield had moderate correlation with  $\text{CH}_4$  production, whereas correlation of MY with  $\text{CH}_4:\text{CO}_2$  ratio was lower.

**Table 1.** Descriptive statistics of CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production

Item	Records (no.)	Cows (no.)	Mean	SD	Minimum	Maximum
CH <sub>4</sub> :CO <sub>2</sub> ratio	3,623	500	0.069	0.013	0.023	0.124
CH <sub>4</sub> production (L/d)	2,202	490	437	119	53	896

### Prediction and Validation

Prediction model results for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production using different trait combinations are shown in Table 3 and Table 4, respectively, and results shown are averages based on 50 random iterations. Spectral data preprocessing using first derivative did not show improvement compared with raw spectra models. Therefore, results shown are based on untreated spectral data.

### CH<sub>4</sub>:CO<sub>2</sub> Ratio and CH<sub>4</sub> Production Prediction

The milk FT-IR full spectral profile (241 wavenumbers) used as predictor traits in CH<sub>4</sub>:CO<sub>2</sub> ratio prediction resulted in low prediction capacity when validated using the external test set for both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production (Tables 3 and 4). Integration of FT-IR along with traits MY and herd showed enhancement in the prediction accuracy of CH<sub>4</sub>:CO<sub>2</sub>; R<sup>2</sup><sub>val</sub> increased from 0.21 to 0.30, and RMSEP decreased from 0.0114 to 0.0107 (Table 3). On the other hand, CH<sub>4</sub> prediction accuracy increased when FT-IR spectra were integrated with MY; R<sup>2</sup><sub>val</sub> increased from 0.13 to 0.35, and RMSEP decreased from 111 to 96 L/d. However, the addition of herd showed a marginal effect (Table 4). For both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production, further addition of the predictor trait lactation stage showed marginal improvement, whereas adding the predictor traits parity and season did not improve accuracy (Tables 3 and 4).

### Selected FT-IR Wavenumbers for CH<sub>4</sub>:CO<sub>2</sub> Ratio and CH<sub>4</sub> Production Prediction

Figure 1a and b illustrates VIP scores and reflects the important FT-IR spectral regions in CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production prediction, respectively. Using the rPLS variable selection method, the 13 most important spectral wavenumbers were identified for CH<sub>4</sub>:CO<sub>2</sub> ratio and the 15 most relevant wavenumbers were selected for CH<sub>4</sub> production. Table 5 provides selected wavenumbers and corresponding chemical functional groups, milk components, feed, and nutrient information. Following the selection of these wavenumbers, they were used to develop prediction models. For CH<sub>4</sub>:CO<sub>2</sub> ratio, this subset of wavenumbers explained 12% of total variation, whereas the full FT-IR spectra explained 21% of the total variation (Table 3). For CH<sub>4</sub> production, the

selected wavenumbers explained 9% of total variation, whereas the full FT-IR spectra explained about 13% of total variation in CH<sub>4</sub> production (Table 4). For both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production, selected wavenumbers corresponded to regions of the milk spectral profile specific to the major milk components fat, protein, and lactose.

When FT-IR predicted fat is used instead of full FT-IR spectra, about 7 and 3% of the variation for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production, respectively, is explained. When FT-IR predicted protein is used, 3 and 7% of variation for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production, respectively, is explained. Combining fat and protein did not improve the prediction accuracy with respect to fat and protein alone for both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production (Tables 3 and 4). That indicates that other spectral wavenumbers related to lactose (carbohydrate) or additional wavenumbers related to fat and protein (amide II) are providing additional variation when using the full spectral profile (Table 3).

## DISCUSSION

The basic assumption underlying multivariate prediction is that measuring phenotypes and variables carries information about the property (predictant or dependent variable) we are seeking to predict (Esbensen, 2000). In the present study, the question of interest is how the CH<sub>4</sub> gas concentration from breath samples is reflected in cow milk composition and thereby in milk FT-IR profile.

### Prediction of CH<sub>4</sub> Emission Based on Milk FT-IR

In general, CH<sub>4</sub> emission is connected to milk FA profile, so one can assume that FT-IR spectral profile could predict CH<sub>4</sub> emission (van Gastelen and Dijkstra, 2016). Several studies have linked individual milk FA to CH<sub>4</sub> emission (Chilliard et al., 2009; van Lingen

**Table 2.** Pearson correlations between different predictor traits and CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production

Trait	CH <sub>4</sub> :CO <sub>2</sub> ratio	CH <sub>4</sub> production (L/d)
Milk yield (kg)	0.23	0.53
Fat (%)	-0.26	-0.18
Protein (%)	-0.17	-0.26
Week of lactation	0.18	0.02

**Table 3.** Partial least squares regression (PLSR) fit statistics for CH<sub>4</sub>:CO<sub>2</sub> ratio<sup>1,2</sup>

Predictor trait <sup>3</sup>	PLSR factors	R <sup>2</sup> <sub>Cal</sub>	R <sup>2</sup> <sub>Val</sub>	RMSEC	RMSEP
MY	1	0.05	0.06	0.0123	0.0126
MY + herd	2	0.14	0.14	0.0117	0.0117
MY + herd + parity	4	0.14	0.14	0.0117	0.0117
MY + herd + parity + lactation stage	5	0.22	0.20	0.0112	0.0113
MY + herd + parity + lactation stage + season	5	0.22	0.21	0.0111	0.0115
Lactation stage	1	0.04	0.04	0.0124	0.0124
IR (full spectra)	12	0.27	0.21	0.0108	0.0114
IR (full spectra) + MY	13	0.30	0.24	0.0106	0.0111
IR (full spectra) + MY + herd	14	0.33	0.30	0.0103	0.0107
IR (full spectra) + MY + herd + parity	14	0.33	0.27	0.0104	0.0108
IR (full spectra) + MY + herd + parity + lactation stage	15	0.35	0.31	0.0098	0.0106
IR (full spectra) + MY + herd + parity + lactation stage + season	15	0.35	0.31	0.0098	0.0105
IR (full spectra) + lactation stage	13	0.27	0.20	0.0108	0.0115
IR (selected 13 wavenumbers)	10	0.14	0.12	0.0117	0.0120
Fat (%)	1	0.06	0.07	0.0123	0.0121
Protein (%)	1	0.03	0.03	0.0124	0.0126
Fat + protein	2	0.07	0.07	0.0122	0.0123
Fat + protein + MY	3	0.09	0.09	0.0121	0.0121

<sup>1</sup>R<sup>2</sup><sub>Cal</sub> = coefficient of determination for calibration; R<sup>2</sup><sub>Val</sub> = coefficient of determination for validation; RMSEC = root mean squared error of calibration; RMSEP = root mean squared error of prediction.

<sup>2</sup>Results are average values from 50 random iterations.

<sup>3</sup>MY = milk yield (kg); IR = mid-infrared.

et al., 2014; Rico et al., 2016). Eskildsen et al. (2014) demonstrated that the FT-IR predictions of milk FA are reliant on indirect correlations, which are confined to covariance structures in the data set. In their study, indirect correlations were found primarily due to the variation associated with total fat content and breed. Also, Shetty et al. (2017) found discrimination between breeds (Holstein and Jersey) in milk FT-IR profile, and it was primarily due to the fat regions of the spectra.

Hoover and Miller (1991) reported that fat and fiber in feed converts to nutrient FA in the rumen, which becomes milk fat. These findings might explain why the fat regions of the milk infrared spectra were informative for both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production prediction (Table 5). However, in the present study, when models were obtained using FT-IR predicted total fat, rather low prediction accuracies were found for both CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production.

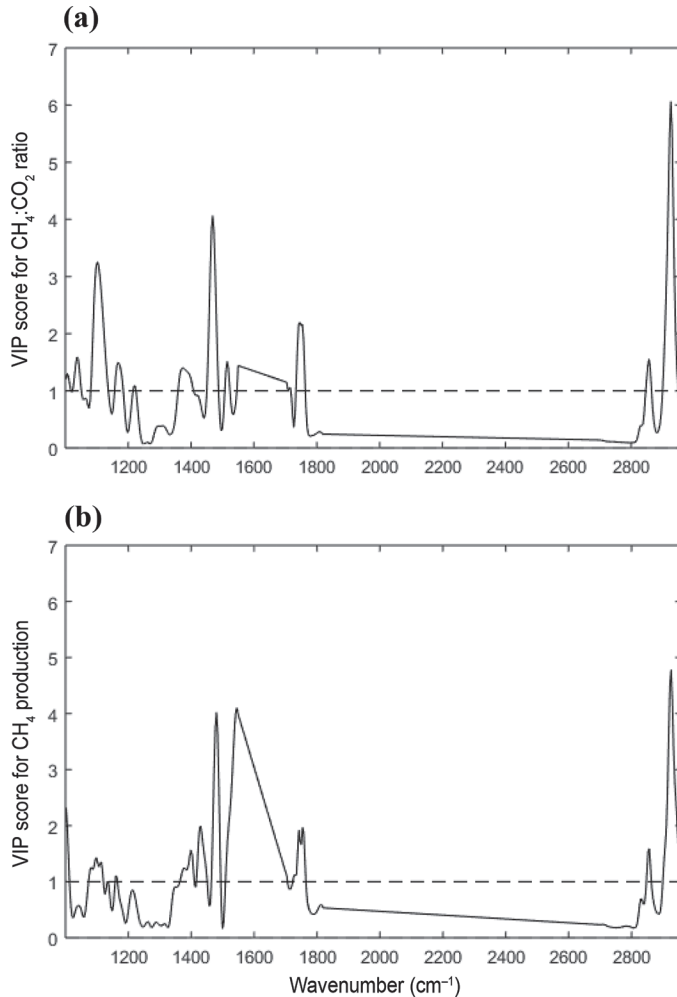
**Table 4.** Partial least squares regression (PLSR) fit statistics for CH<sub>4</sub> production (L/d)<sup>1,2</sup>

Predictor trait <sup>3</sup>	PLSR factors	R <sup>2</sup> <sub>Cal</sub>	R <sup>2</sup> <sub>Val</sub>	RMSEC	RMSEP
MY	1	0.28	0.27	101	102
MY + herd	2	0.32	0.33	98	99
MY + herd + parity	4	0.33	0.31	98	98
MY + herd + parity + lactation stage	5	0.36	0.36	96	95
MY + herd + parity + lactation stage + season	5	0.37	0.36	95	95
Lactation stage	1	0.05	0.05	116	119
IR (full spectra)	12	0.21	0.13	106	111
IR (full spectra) + MY	13	0.39	0.35	93	96
IR (full spectra) + MY + herd	14	0.42	0.37	91	94
IR (full spectra) + MY + herd + parity	14	0.41	0.37	91	94
IR (full spectra) + MY + herd + parity + lactation stage	15	0.42	0.39	90	94
IR (full spectra) + MY + herd + parity + lactation stage + season	15	0.44	0.39	89	94
IR (full spectra) + lactation stage	13	0.22	0.14	105	112
IR (selected 15 wavenumbers)	10	0.12	0.09	112	115
Fat (%)	1	0.03	0.03	117	119
Protein (%)	1	0.07	0.07	115	115
Fat + protein	2	0.07	0.07	115	113
Fat + protein + MY	3	0.28	0.27	112	113

<sup>1</sup>R<sup>2</sup><sub>Cal</sub> = coefficient of determination for calibration; R<sup>2</sup><sub>Val</sub> = coefficient of determination for validation; RMSEC = root mean squared error of calibration; RMSEP = root mean squared error of prediction.

<sup>2</sup>Results are average values from 50 random iterations.

<sup>3</sup>MY = milk yield (kg); IR = mid-infrared.



**Figure 1.** Variable importance for projection (VIP) scores of (a)  $\text{CH}_4:\text{CO}_2$  ratio and (b)  $\text{CH}_4$  production (L/d) plotted against wavenumber ( $\text{cm}^{-1}$ ).

Currently, 2 studies have investigated prediction of  $\text{CH}_4$  emission of individual cows directly using FT-IR spectral profile. Dehareng et al. (2012) used 11 lactating Holstein cows in 2 experiments and 3 dietary treatments. The prediction accuracy of models developed for  $\text{CH}_4$  production (g/d) and  $\text{CH}_4$  milk (g/kg of milk) on this small data set is somewhat high; the cross-validated coefficient of determination ranged from 0.68 to 0.79. In another study, lactation stage-dependent prediction models of  $\text{CH}_4$  emission from FT-IR spectral profile were developed using 532  $\text{CH}_4$  measurements of 165 Holstein, Jersey, and Holstein-Jersey cows and had a cross-validated  $R^2$  of 0.70 (Vanlierde et al., 2015, 2016). Conversely, in the present study much lower prediction accuracies were obtained when models were developed using FT-IR spectra alone as well as integration with the lactation stage information for both  $\text{CH}_4:\text{CO}_2$  ratio and  $\text{CH}_4$  production.

The large discrepancy in prediction accuracies between the aforementioned studies and the present study is of concern. Possible sources of the discrepancy could be differences in the methods used to measure  $\text{CH}_4$  emission, the size and structure of the populations, prediction and validation methods, or some combination of these. In Dehareng et al. (2012) and Vanlierde et al. (2015, 2016),  $\text{CH}_4$  emission was measured using the sulfur hexafluoride ( $\text{SF}_6$ ) tracer method, whereas the present study used sniffers installed in AMS and  $\text{CO}_2$  as a tracer gas. The 2 methods have not been compared directly; however, both have been benchmarked against the intensive respiration chamber method. McGinn et al. (2006) found an  $R^2_{\text{Val}}$  of 0.80 and a concordance correlation coefficient of 0.79 between the  $\text{SF}_6$  method and respiration chambers for 8 beef heifers. Garnsworthy et

**Table 5.** Recursive weighted partial least squares regression selected important spectral wavenumbers for  $\text{CH}_4:\text{CO}_2$  ratio and  $\text{CH}_4$  production (L/d) along with corresponding chemical functional groups, milk components, feed, and nutrient information

Wavenumber ( $\text{cm}^{-1}$ )	Milk components	Nutrients	Feed	Functional group
<b><math>\text{CH}_4:\text{CO}_2</math> ratio</b>				
2,957, 2,953, 2,876	Fat B <sup>1</sup>	Fatty acids, acetic, butyric	Fermentable fiber	Alkyl chain (C-H)
1,727	Fat A <sup>1</sup>	Fatty acids, acetic, butyric	Fermentable fiber	Carbonyl group (C=O)
1,376	Protein (amide II)	AA	CP	Aromatic amines (N-H)
1,249	Protein (amide III)	AA	CP	Aromatic amines (C-N)
1,172, 1,137, 1,099, 1,076, 1,068, 1,064, 1,002	Lactose (carbohydrate)	Propionic (glucose)	Sugar, starch	Hydroxyl group (O-H)
<b><math>\text{CH}_4</math> production (L/d)</b>				
2,957, 2,953, 2,826	Fat A <sup>1</sup>	Fatty acids, acetic, butyric	Fermentable fiber	Alkyl chain (C-H)
1,519	Protein (amide II)	AA	CP	Aromatic amines (N-H)
1,276	Protein (amide III)	AA	CP	Aromatic amines (C-N)
1,195, 1,130, 1,099, 1,083, 1,079, 1,072, 1,068, 1,064, 1,056, 1,029	Lactose (carbohydrate)	Propionic (glucose)	Sugar, starch	Hydroxyl group (O-H)

<sup>1</sup>The measurement of fat by milk Fourier transform mid-infrared spectra used the carbonyl stretch (C=O), which has been called fat A, and the symmetrical carbon hydrogen stretch (C-H), which has been called fat B, in the Fourier transform mid-infrared spectral region (Biggs et al., 1987; Barbano and Clark, 1989).

al. (2012) found measurements from the NDIR installed in the AMS to have an  $R^2_{\text{val}}$  of 0.79 with subsequent measurements in respiration chambers for 12 Holstein cows. Likewise, Negussie et al. (2017) found  $\text{CH}_4$  emissions using a photoacoustic infrared sniffer and  $\text{CO}_2$  as a tracer gas to have a high concordance (concordance correlation coefficient = 0.71) and an  $R^2_{\text{val}}$  of 0.70 in 21 Nordic Red cows. Haque et al. (2014) found  $\text{CH}_4$  emissions from FT-IR installed in AMS and  $\text{CO}_2$  as a tracer gas to have statistical power equivalent to  $\text{SF}_6$ . Based on these findings, one could expect some decrease in prediction accuracy using  $\text{CH}_4$  emission from sniffers and  $\text{CO}_2$  as a tracer gas, but not to the extent observed.

The present method of estimating  $\text{CH}_4$  emission is based on 3 components: the measured ratio of gases, estimation of heat production units (**HPU**), and the conversion of HPU to  $\text{CO}_2$  production. However, the specific accuracies of these components have yet to be evaluated and their relative contributions to  $\text{CH}_4$  emission accuracy have yet to be quantified. It is important to note that the most influential predictor of HPU is ECM, which is milk production corrected for fat, protein, and lactose percentages estimated from FT-IR spectra. Based on this, one would expect some autocorrelations, resulting in higher accuracies of prediction  $\text{CH}_4$  emission from sniffers and  $\text{CO}_2$  tracer gases predicted from FT-IR spectra.

A further difference between the present and aforementioned studies (Dehareng et al., 2012; Vanlierde et al., 2015, 2016) is the duration of measurement and time between  $\text{CH}_4$  measurements and milk FT-IR sampling. In the present study, weekly averaged  $\text{CH}_4$  measurements were predicted from corresponding weekly averaged milk FT-IR spectra of an experimental farm and commercial farms from a single milk FT-IR falling within the week of  $\text{CH}_4$  measurement, whereas Dehareng et al. (2012) and Vanlierde et al. (2015, 2016) used daily  $\text{CH}_4$  measurements to perform the prediction models from milk FT-IR spectra averaged from the morning and afternoon milkings on each measurement day. Logically, reducing the time between milk FT-IR and  $\text{CH}_4$  measurements should maximize the biological relationships on which the prediction equations are built. However, Moate et al. (2012) found that the DMI of the preceding day to  $\text{CH}_4$  measurement is responsible for 30% of the variation in  $\text{CH}_4$  on the day of measurement. Moreover,  $\text{CH}_4$  measurements have been shown to be more stable when averaged over 3 to 5 consecutive days for  $\text{SF}_6$  (Deighton et al., 2014; Arbore et al., 2016) and for 1 wk for the sniffer method (Difford et al., 2016). Thus, further work is needed to determine the optimization between maximizing the stability of the  $\text{CH}_4$  measurement and minimizing the time between representative  $\text{CH}_4$  measurements and

FT-IR milk spectra and their respective effects on milk FT-IR prediction of  $\text{CH}_4$  emission.

In Dehareng et al. (2012) and Vanlierde et al. (2015, 2016), cows were fed a variety of diets within different experimental conditions in different countries to maximize the variability of individual  $\text{CH}_4$  emission and thereby increase the spectral variability required for a robust calibration model. However, instances where experimental treatments affect  $\text{CH}_4$  emission as well as milk composition induce covariance structure into the data set and can inflate the prediction accuracies when not properly accounted for in the validation method. In contrast, the current study used a larger sample of Holstein cows from both experimental and commercial farms fed a TMR used in commercial practice. This sampling strategy is more representative of animals and conditions in the national Danish population and is less likely to suffer from induced covariance structure caused by extraneous factors coaffecting  $\text{CH}_4$  emission and milk composition.

For robust FT-IR predictions, the indirect covariance structures in the calibration data set must be valid for future new samples (Eskildsen et al., 2014). In the present study, models developed were validated using an independent (data not used in the calibration model) or external test set by leaving out records of 20% cows for validation and keeping records of 80% cows for training the model with 50 random iterations. In Dehareng et al. (2012) and Vanlierde et al. (2015, 2016), models were validated using a cross-validation method. In cross-validation, data are divided into complementary subsets, training the model on one subset and validating on the other subset for a specific fold. However, if no precautions are taken, the same cow could have records in both training and validation sets for this specific fold. This may result in overfitted prediction models, more so if there is unaccounted experimental treatment structure within the data. In the present study, additional validations were performed (results not shown) to ensure that the obtained model is robust in predicting new data sets of similar types. On one hand, experimental farm data were used to build the training model and cross-validation was performed to evaluate the model performance for  $\text{CH}_4$ : $\text{CO}_2$  ratio and  $\text{CH}_4$  production; results showed that similar coefficient of determination values were found for both calibration and cross-validation. On the other hand, the obtained model using experimental farm data was evaluated using commercial farm data, which is a completely independent test set; results showed negligible  $R^2_{\text{val}}$  compared with coefficients of determination for calibration for both  $\text{CH}_4$ : $\text{CO}_2$  ratio and  $\text{CH}_4$  production, indicating that variation in commercial farm data is not included in the experimental data.

### **Prediction of CH<sub>4</sub> Emission Based on Factors Other than FT-IR Spectra**

In their study, van Gastelen and Dijkstra (2016) suggested that integration of other factors such as nutrient composition of the feed, parity, and lactation stage along with FT-IR spectra may improve the prediction of CH<sub>4</sub> emission. In the present study, traits such as MY, herd, parity, lactation stage, and season along with FT-IR profiles were used as predictor traits. For the CH<sub>4</sub>:CO<sub>2</sub> ratio prediction model, factors MY, herd, and lactation stage along with FT-IR spectra showed improvement; however, overall prediction accuracy still remained modest (Tables 3 and 4). For CH<sub>4</sub> production prediction, integration of FT-IR along with the aforementioned traits showed only a marginal improvement (Table 4). These results indicated that FT-IR profile reflected primarily information related to MY, herd, and lactation stage rather than relevant individual milk FA, which are generally assumed to be connected to CH<sub>4</sub> emission. In Vanlierde et al. (2015, 2016), CH<sub>4</sub> predictions using FT-IR spectra alone were compared with CH<sub>4</sub> predictions using FT-IR spectra and lactation stage information. The models were hardly different and had a cross-validated R<sup>2</sup> of 0.70 (vs. 0.67) and a standard error of cross-validation of 66 g/d (vs. 63). However, in contrast with the prediction using FT-IR spectra only, the lactation stage-dependent model showed biologically meaningful CH<sub>4</sub> values (i.e., an increase in CH<sub>4</sub> production between 0 and 100 DIM and a decrease thereafter). The present study also showed only marginal improvement when adding lactation stage information along with FT-IR spectra. Obtained prediction accuracies were much lower in the current study (Tables 3 and 4); therefore, it was not possible to confirm the advantage of the lactation stage-dependent model.

### **CONCLUSIONS**

In the present study, feasibility of FT-IR spectroscopy of milk in predicting CH<sub>4</sub> emission is elucidated. Low prediction accuracies were obtained for CH<sub>4</sub>:CO<sub>2</sub> ratio and CH<sub>4</sub> production when models were obtained using FT-IR spectra. When models were integrated with other factors such as MY, herd, and lactation stage, results showed improvement in the prediction accuracy; however, overall prediction accuracy still remained modest. For CH<sub>4</sub> production prediction added value of the FT-IR along with the aforementioned traits was marginal. This implies that for CH<sub>4</sub> production prediction, FT-IR profiles reflect primarily information related to MY, herd, and lactation stage rather than relevant individual milk FA, which are generally as-

sumed to be connected to CH<sub>4</sub> emission. Therefore, it is not feasible to predict CH<sub>4</sub> emission based on FT-IR spectra alone. Moreover, the present study uses weekly averaged milk FT-IR spectra to predict weekly averaged CH<sub>4</sub> measurements. Improving CH<sub>4</sub> measurement may improve the accuracy of its prediction using FT-IR spectra. Thus, further work is needed to determine the optimization between maximizing the stability of the CH<sub>4</sub> measurements and minimizing the time between representative CH<sub>4</sub> measurements and FT-IR milk spectra.

### **ACKNOWLEDGMENTS**

This study was financially supported by two projects: “FT-IR spektre i mælk: Genetisk variation og effekt på sundhed, frugtbarhed og energibalance” of the Milk Levy Fund, Denmark (2015–2017), and Robust and Efficient Dairy Cows, project no. 34009-14-0848 of Grønt Udviklings- og Demonstrations Program (2015–2018). The authors thank the Foundation for Registration and Milk Recording (Aarhus, Denmark) for providing data.

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